

WHAT IS CLAIMED IS:

1. A computational image model, comprising:
an image support including a structure of n-pixels comprising pixel
5 faces;
quantities related to image features; and
an algebraic structure relating the quantities to the n-pixels and/or pixel
faces, the algebraic structure comprising algebraic operations defining a
relation between the quantities.
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2. A computational image model as defined in claim 1, wherein each n-
pixel is defined as a geometrical structure comprising vertices, edges, faces
and a volume, and wherein each n-pixel comprises:
a first pixel dimension $n=0$ including the vertices of the n-pixel;
15 a second pixel dimension $n=1$ including the edges of the n-pixel;
a third pixel dimension $n=2$ including the faces of the n-pixel;
a fourth pixel dimension $n=3$ including the volume of the n-pixel; and
a n^{th} pixel dimension n including the hypervolume of the n-pixel.
- 20 3. A computational image model as defined in claim 1, wherein the
geometrical structure is selected from the group consisting of: a cube, a
triangle, a hexagone and a pentagone.
4. A computational image model as defined in claim 1, wherein the
25 quantities related to image features are selected from the group consisting of:
scalar quantities, vectors, tensors and matrices.
5. A computational image model as defined in claim 1, wherein the
algebraic operations comprise problem-independent operations.
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6. A computational image model as defined in claim 1, wherein the
algebraic operations comprise problem-dependent operations.

7. A computational image model as defined in claim 1, wherein the structure of n-pixels comprises pairs of disjoint n-pixels.

5 8. A computational image model as defined in claim 1, wherein the structure of n-pixels comprises pairs of n-pixels intersecting through a common i-pixel, where $i < n$.

9. A computational image model as defined in claim 1, wherein each n-pixel is translated algebraically into a q-pixel, wherein $q \in \{1, 2, \dots, n\}$.

10. A computational image model as defined in claim 9, wherein each q-pixel includes (q-1)-faces, (q-2)-faces, ..., (q-q)-faces.

15 11. A computational image model as defined in claim 9, wherein the image support comprises a geometrical complex, which is a collection of q-pixels.

12. A computational image model as defined in claim 10, wherein the image support comprises a geometrical complex, which is a collection of q-pixels, and wherein:

- every face of a q-pixel in the geometrical complex is also located in the geometrical complex; and
- any pair of two q-pixels of the geometrical complex have an intersection which is either empty or constituted by a common face of both q-pixels of the pair.

13. A computational image model as defined in claim 11, comprising a plurality of image supports forming the geometrical complex.

14. A computational image model as defined in claim 11, wherein the geometrical complex is expressed in algebraic form as a q-chain, which is a linear combination of all the q-pixels of the geometrical complex.

5 15. A computational image model as defined in claim 9, wherein the geometrical complex comprises q-cochains, which are relations associating quantities related to image features to the q-pixels and/or faces of said q-pixels.

10 16. A computational image model as defined in claim 15, wherein the quantities related to image features and associated to the q-pixels and/or faces of said q-pixels are global quantities associated to all the q-pixels.

15 17. A computational image model as defined in claim 15, wherein the quantities related to image features and associated to the q-pixels and/or faces of said q-pixels are local quantities each associated to one q-pixel and/or faces of said one q-pixel.

20 18. A computational image model as defined in claim 16, comprising $(q \geq 1)$ -cochains to represent the local quantities.

 19. A computational image model as defined in claim 17, comprising 0-cochain to represent the global quantities.

25 20. A computational image model as defined in claim 17, wherein the algebraic operations comprise a coboundary operation giving a relationship between the q-cochains.

30 21. A computational image model as defined in claim 9, wherein:
the image support comprises a plurality of geometrical complexes, each being a collection of q-pixels; and

the algebraic operations comprise a codual operation establishing a link between q-cochains that belong to different geometrical complexes.

22. A method of computationally modelling an image, comprising:
5 producing an image support including a structure of n-pixels comprising pixel faces;
defining quantities related to image features; and
relating the quantities to the n-pixels and/or pixel faces through an algebraic structure, and relating the quantities to each other through algebraic
10 operations.

23. A method of computationally modelling an image as defined in claim 22, wherein relating the quantities to the n-pixels and/or pixel faces through an algebraic structure comprises translating each n-pixel algebraically
15 into a q-pixel, wherein $q \in \{1, 2, \dots, n\}$, wherein each q-pixel includes (q-1)-faces, (q-2)-faces, ..., (q-q)-faces.

24. A method of computationally modelling an image as defined in claim 22, wherein producing an image support comprises forming a
20 geometrical complex, which is a collection of q-pixels, and wherein:
- every face of a q-pixel in the geometrical complex is also located in the geometrical complex; and
- any pair of two q-pixels of the geometrical complex have an intersection which is either empty or constituted by a common face of both q-pixels
25 of the pair.

25. A method of computationally modelling an image as defined in claim 24, wherein producing an image support comprises forming a plurality of image supports forming the geometrical complex.

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26. A method of computationally modelling an image as defined in claim 24, wherein relating the quantities to the n-pixels and/or pixel faces

through an algebraic structure comprises expressing the geometrical complex in algebraic form as a q-chain, which is a linear combination of all the q-pixels of the geometrical complex.

5 27. A method of computationally modelling an image as defined in claim 24, wherein relating the quantities to the n-pixels and/or pixel faces through an algebraic structure comprises forming, in the geometrical complex, q-cochains which are relations associating quantities related to image features to the q-pixels and/or faces of said q-pixels.

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 28. A method of computationally modelling an image as defined in claim 22, wherein defining quantities related to image features comprises defining global quantities associated to all the q-pixels.

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 29. A method of computationally modelling an image as defined in claim 22, wherein defining quantities related to image features comprises defining local quantities associated to one q-pixel and/or faces of said one q-pixel.

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 30. A method of computationally modelling an image as defined in claim 27, wherein relating the quantities to each other through algebraic operations comprise producing a coboundary operator giving a relationship between q-cochains.

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 31. A method of computationally modelling an image as defined in claim 27, wherein:

 producing an image support comprises forming a plurality of geometrical complexes, each being a collection of q-pixels; and

 relating the quantities to each other through algebraic operations
30 comprises producing a codual operation establishing a link between cochains that belong to different geometrical complexes.

32. An image modelling method as defined in claim 27, wherein relating the quantities to the n-pixels and/or pixel faces through an algebraic structure comprises expressing a global quantity associated with all q-pixels through a q-cochain such that, for two adjacent q-pixels c_q^1 and c_q^2 , the q-cochain F_q satisfies the relation $F_q(\lambda_1 c_q^1 + \lambda_2 c_q^2) = \lambda_1 F_q(c_q^1) + \lambda_2 F_q(c_q^2)$, where λ_1 and λ_2 are integers.

33. An image modelling method as defined in claim 22, wherein:
- relating the quantities to the n-pixels and/or pixel faces through an algebraic structure comprises translating each n-pixel algebraically into a q-pixel, wherein $q \in \{1, 2, \dots, n\}$, wherein each q-pixel includes (q-1)-faces, (q-2)-faces, ..., (q-q)-faces;
 - producing an image support comprises forming geometrical complexes, each being a collection of q-pixels;
 - relating the quantities to the n-pixels and/or pixel faces through an algebraic structure comprises:
 - o expressing each geometrical complex in algebraic form as a q-chain, which is a linear combination of all the q-pixels of the geometrical complex;
 - o forming, in the geometrical complexes, q-cochains which are relations associating quantities related to image features to the q-pixels and/or faces of said q-pixels;
 - relating the quantities to each other through algebraic operations comprises:
 - o producing a coboundary operator giving a relationship between the q-cochains; and
 - o producing a codual operation establishing a link between q-cochains that belong to different geometrical complexes.

34. A computational framework for solving a problem using an image computationally modelled by means of the method of claim 33, comprising:

identifying basic laws associated to the problem;
from the identified basic laws, defining quantities related to the problem;
associating the quantities to respective q-cochains;
associating the basic laws related to the problem to respective
5 coboundary and codual operations; and
resolving the resulting algebraic system.

35. A computational framework as defined in claim 34, wherein forming
geometrical complexes comprises forming first and second geometrical
10 complexes.

36. A computational framework as defined in claim 35, wherein
identifying basic laws associated to the problem comprises supporting one
basic law through the first geometrical complex.

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37. A computational framework as defined in claim 36, wherein the
problem to be solved is a 2D global differential equation for heat flow in a
homogeneous medium, and wherein said one basic law is a heat flow law.

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38. A computational framework as defined in claim 37, wherein
associating the quantities to respective q-cochains comprises representing a
global quantity of temperature through a 0-cochain, and associating the heat
flow law through a 1-cochain.

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39. A computational framework as defined in claim 35, wherein
identifying basic laws associated to the problem comprises supporting one
basic law through the second geometrical complex.

40. A computational framework as defined in claim 39, wherein the
30 problem to be solved is a 2D global differential equation for heat flow in a
homogeneous medium, and wherein said one basic law is a heat source law.

41. A computational framework as defined in claim 36, wherein identifying basic laws associated to the problem comprises supporting a second basic law through the second geometrical complex, and wherein associating the basic laws related to the problem to respective coboundary and codual operations comprises representing a constitutive law linking basic laws from the first and second geometrical complexes by a codual operation.

42. An image modelling method as defined in claim 22, wherein:

- relating the quantities to the n-pixels and/or pixel faces through an algebraic structure comprises translating each n-pixel algebraically into a q-pixel, wherein $q \in \{1, 2, \dots, n\}$, wherein each q-pixel includes (q-1)-faces, (q-2)-faces, ..., (q-q)-faces;
- producing an image support comprises forming a geometrical complex, which is a collection of q-pixels;
- relating the quantities to the n-pixels and/or pixel faces through an algebraic structure comprises:
 - o expressing the geometrical complex in algebraic form as a q-chain, which is a linear combination of all the q-pixels of the geometrical complex;
 - o forming, in the geometrical complex, q-cochains which are relations associating quantities related to image features to the q-pixels and/or faces of said q-pixels;
- relating the quantities to each other through algebraic operations comprises:
 - o producing coboundary operations giving a relationship between the q-cochains.

43. A computational framework for solving a problem using an image computationally modelled by means of the method of claim 42, comprising:

- identifying basic laws associated to the problem;
- from the identified basic laws, defining quantities related to the problem;
- associating the quantities to respective q-cochains;

associating the basic laws related to the problem to respective coboundary operations; and
resolving the resulting algebraic system.

5 44. A computational framework for solving a heat transfer problem, comprising:

producing an image support including a structure of n-pixels, the image support comprising:

- 10 ○ q-pixels respectively translating the n-pixel algebraically, wherein $q \in \{1, 2, \dots, n\}$, and wherein each q-pixel includes (q-1)-faces, (q-2)-faces, ..., (q-q)-faces;
- geometrical complexes each being a collection of q-pixels;
- q-chains respectively expressing the geometrical complexes in algebraic form, each q-chain being a linear combination of all
15 the q-pixels of the geometrical complex;
- in the geometrical complexes, q-cochains which are relations associating quantities related to image features to the q-pixels and/or faces of said q-pixels; and
- a coboundary defining a relation between q-cochains;

20 computing a q-cochain T of a first of said geometrical complexes as the location of unknown temperatures;

 computing a q-cochain H of the first geometrical complex as a global temperature variation;

25 finding a q-cochain ε of a second geometrical complex as a global energy variation, as a function of the q-cochain H through a linear transformation;

 finding the q-cochain ε as a function of the q-cochain T;

30 defining a q-cochain G of the first geometrical complex from the q-cochain T through a first coboundary operation, transforming the q-cochain G into a q-cochain Q of the second geometrical complex, and defining, from the q-cochain Q and through a second coboundary operation, a q-cochain D of the second geometrical complex as a global diffusion;

defining a q-cochain S of the second geometrical complex as a global source; and

establishing a relation between the q-cochains ε , D and S .

5 45. A computational framework for two-dimensional active contour model, comprising:

producing an image support including a structure of n-pixels, the image support comprising:

- 10 - q-pixels respectively translating the n-pixel algebraically, wherein $q \in \{1, 2, \dots, n\}$, and wherein each q-pixel includes (q-1)-faces, (q-2)-faces, ..., (q-q)-faces;
- geometrical complexes each being a collection of q-pixels;
- q-chains respectively expressing the geometrical complexes in algebraic form, each q-chain being a linear combination of
- 15 all the q-pixels of the geometrical complex;
- in the geometrical complexes, q-cochains which are relations associating quantities related to image features to the q-pixels and/or faces of said q-pixels; and
- a coboundary defining a relation between q-cochains;

20 computing a displacement q-cochain D of a first of said geometrical complexes;

 computing a strain q-cochain S of a second of said geometrical complexes, comprising:

- 25 - defining an approximate strain function $\tilde{\varepsilon}(x)$ as a function of the q-cochain D ;
- expressing the q-cochain S as a function of the approximate strain function and relative positions of the first and second geometrical complexes; and

 computing a force q-cochain F of the second geometrical complex as a

30 coboundary of the strain q-cochain S .